

6-2019

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Giuseppe Lodato
Università degli Studi di Milano

Giovanni Dipierro
University of Leicester

Enrico Ragusa
Università degli Studi di Milano

Feng Long
Peking University

Gregory J. Herczeg
Peking University

See next page for additional authors

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Recommended Citation

Lodato, Giuseppe; Dipierro, Giovanni; Ragusa, Enrico; Long, Feng; Herczeg, Gregory J.; Pascucci, Ilaria; Pinilla, Paola; Manara, Carlo F.; Tazzari, Marco; Liu, Yao; Mulders, Gijs D.; Harsono, Daniel; Boehler, Yann; Ménard, François; Johnstone, Doug; Salyk, Colette; van der Plas, Gerrit; Cabrit, Sylvie; Edwards, Suzan; Fischer, William J.; Hendl, Nathan; Nisini, Brunella; Rigliaco, Elisabetta; Avenhaus, Henning; Banzatti, Andrea; and Gully-Santiago, Michael, "The Newborn Planet Population Emerging from Ring-Like Structures in Discs" (2019). Astronomy: Faculty Publications, Smith College, Northampton, MA. https://scholarworks.smith.edu/ast_facpubs/11

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Authors

Giuseppe Lodato, Giovanni Dipierro, Enrico Ragusa, Feng Long, Gregory J. Herczeg, Ilaria Pascucci, Paola Pinilla, Carlo F. Manara, Marco Tazzari, Yao Liu, Gijs D. Mulders, Daniel Harsono, Yann Boehler, François Ménard, Doug Johnstone, Colette Salyk, Gerrit van der Plas, Sylvie Cabrit, Suzan Edwards, William J. Fischer, Nathan Hendler, Brunella Nisini, Elisabetta Rigliaco, Henning Avenhaus, Andrea Banzatti, and Michael Gully-Santiago

The newborn planet population emerging from ring-like structures in discs

Giuseppe Lodato ¹★, Giovanni Dipierro ², Enrico Ragusa ^{1,2}, Feng Long, ³ Gregory J. Herczeg, ³ Ilaria Pascucci, ^{4,5} Paola Pinilla, ⁶ Carlo F. Manara, ⁷ Marco Tazzari ⁸, Yao Liu, ^{9,10} Gijs D. Mulders, ^{5,11} Daniel Harsono, ¹² Yann Boehler, ¹³ François Ménard, ¹³ Doug Johnstone, ^{14,15} Colette Salyk, ¹⁶ Gerrit van der Plas, ¹³ Sylvie Cabrit, ¹⁷ Suzan Edwards, ¹⁸ William J. Fischer, ¹⁹ Nathan Hendler, ⁴ Brunella Nisini, ²⁰ Elisabetta Rigliaco, ²¹ Henning Avenhaus, ⁹ Andrea Banzatti ⁴ and Michael Gully-Santiago ²²

Affiliations are listed at the end of the paper

Accepted 2019 March 25. Received 2019 March 12; in original form 2018 November 23

ABSTRACT

ALMA has observed a plethora of ring-like structures in planet-forming discs at distances of 10–100 au from their host star. Although several mechanisms have been invoked to explain the origin of such rings, a common explanation is that they trace new-born planets. Under the planetary hypothesis, a natural question is how to reconcile the apparently high frequency of gap-carving planets at 10–100 au with the paucity of Jupiter-mass planets observed around main-sequence stars at those separations. Here, we provide an analysis of the new-born planet population emerging from observations of gaps in discs, under the assumption that the observed gaps are due to planets. We use a simple estimate of the planet mass based on the gap morphology, and apply it to a sample of gaps recently obtained by us in a survey of Taurus with ALMA. We also include additional data from recent published surveys, thus analysing the largest gap sample to date, for a total of 48 gaps. The properties of the purported planets occupy a distinctively different region of parameter space with respect to the known exo-planet population, currently not accessible through planet finding methods. Thus, no discrepancy in the mass and radius distribution of the two populations can be claimed at this stage. We show that the mass of the inferred planets conforms to the theoretically expected trend for the minimum planet mass needed to carve a dust gap. Finally, we estimate the separation and mass of the putative planets after accounting for migration and accretion, for a range of evolutionary times, finding a good match with the distribution of cold Jupiters.

Key words: accretion, accretion discs—planets and satellites: formation—protoplanetary discs.

1 INTRODUCTION

The discovery of the HL Tau disc and its system of rings (ALMA Partnership et al. 2015) has marked a new era in our understanding of the gas and dust discs around young stellar objects. Disc substructures appear to be commonplace, and in particular, the most frequently observed structures are regular, almost axisymmetric rings (Andrews et al. 2016; Isella et al. 2016; Fedele et al. 2017, 2018; Clarke et al. 2018; Dipierro et al. 2018; Hendler et al. 2018;

van Terwisga et al. 2018; Liu et al. 2019). Many theoretical models have been proposed to explain the origin of such rings, including dead zones (Ruge et al. 2016), condensation fronts (Zhang, Blake & Bergin 2015), self-induced dust pile-ups (Gonzalez et al. 2015), self-induced reconnection in magnetized disc-wind systems (Suriano et al. 2018) or large-scale vortices (Barge et al. 2017). However, another natural explanation is to associate the gap in the disc to the presence of an embedded planet (Huang et al. 2018; Long et al. 2018). This hypothesis has been tested extensively by comparing the disc emission obtained from ALMA observations to that computed from detailed hydrodynamical and radiative transfer simulations (e.g. Dipierro et al. 2015; Clarke et al. 2018).

* E-mail: giuseppe.lodato@unimi.it

Several questions arise, however, if one assumes a planetary origin for gaps in discs. In particular, gaps are typically observed at radial distances from the star of the order of 10–100 au (Zhang et al. 2016). It is therefore natural to ask how to reconcile this evidence with the lack of Jupiter-mass planets at such distances around main-sequence stars, as apparent from the extensive planet-detection campaigns of the last decade (Bowler & Nielsen 2018). In order to understand the orbital and physical evolution of planets from birth to adulthood, we need to compare the properties of planets around T Tauri stars and young stellar objects to those of planets around main-sequence stars. Such a comparison is not easy because usually the planet properties in gapped discs are obtained through complex and time-consuming numerical simulations, which are not feasible for large samples, and are sensitive to several physical parameters (dust–gas coupling, disc thermodynamics, etc.), for which specific assumptions need to be made.

In this paper, we provide an analysis of the properties of the newborn planet population, as implied from a sample of gaps and rings detected in our recent survey of discs in the Taurus–Auriga star-forming region. To this end, we use a simple prescription to relate the observed width of the gap to the mass of planet assumed to be responsible for its opening. We then relate the resulting planetary properties to the stellar properties and to the population of known exo-planets.

This paper is organized as follows. In Section 2, we describe the simple method we use to give an estimate of the planet mass based on the gap morphologies. In Section 3, we show our main results. In Section 4, we draw our conclusions.

2 PLANET PROPERTIES FROM DISC GAPS

Recently, Long et al. (2018) investigated a subsample of 12 discs showing substructures within a larger sample of 32 discs in Taurus obtained with ALMA Band 6 (at 1.3 mm) in Cycle 4 (ID: 2016.1.01164.S; PI: Herczeg). The sample selection will be fully described by Long et al. (in preparation). Briefly, the sample was selected from stars in Taurus with spectral types earlier than M3 and with line-of-sight extinctions < 3 mag. The selection was unbiased to the disc mm flux and to any previously known disc structures from mid-IR photometry; the primary bias is the exclusion of discs that had been previously imaged with ALMA at high spatial resolution. Some of these discs show multiple rings and gaps, providing us with a total of 15 gaps with known morphologies (excluding four additional discs with inner cavities). In Table 1, we provide a summary of the gap properties relevant to this study. A more detailed analysis can be found in Long et al. (2018).

Numerical simulations of gas and dust are the best tool to constrain the planetary properties that reproduce a given structure in a disc. However, such numerical simulations are very time consuming to determine the planetary properties for our sizable sample of discs. Instead, we use empirically determined scaling relations between the gap properties and the planetary mass. In particular, for low-viscosity discs ($\alpha \lesssim 0.01$), the gap width Δ (defined here as the distance between the location of the brightness minimum in the gap and the ring peak, see Long et al. 2018) is expected to scale with the planet Hill radius

$$R_H = \left(\frac{M_p}{3M_*} \right)^{1/3} R, \quad (1)$$

where R is the planet position (assumed here to coincide with the gap location), with a proportionality constant ranging from 4 to 8 depending on the disc parameters, so that $\Delta = kR_H$ (Dodson-

Robinson & Salyk 2011; Pinilla, Benisty & Birnstiel 2012; Fung & Chiang 2016; Rosotti et al. 2016; Facchini et al. 2018). Note that here we assume a one-to-one correspondence between a gap and a planet, while there is the possibility that multiple planets open a common single gap (Zhu et al. 2011) or that a single planet might open multiple gaps (Dong et al. 2018). Finally, note that the gap width likely depends somewhat on disc hydrodynamical properties, such as pressure and viscosity (Pinilla et al. 2012; Fung, Shi & Chiang 2014).

Two discs in our sample, MWC480 (Liu et al. 2019) and CI Tau (Clarke et al. 2018), have been simulated with detailed hydrodynamical simulations to reproduce the gap properties. MWC 480 presents a gap at ~ 73 au, which has been reproduced with a $2.3 M_{\text{Jup}}$ planet in the hydro simulations of Liu et al. (2019). The observed width of the gap in MWC 480 corresponds to $\sim 4.5 R_H$. CI Tau presents three gaps at ~ 14 , 48, and 120 au from the central star. Higher resolution observations of this system were obtained by Clarke et al. (2018), who model the three gaps with three planets with 0.75, 0.15, and $0.4 M_{\text{Jup}}$. It should be noted that the gap widths observed in Clarke et al. (2018) are not easily comparable to the ones measured by Long et al. (2018), due to the different functional form of the radial dust profile used and in particular due to the fact that Clarke et al. (2018) use different inner and outer gap width, as opposite to the symmetrical Gaussian employed in Long et al. (2018). Despite these differences, the two outermost gaps appear to have a comparable normalized width in the two studies, while the innermost one is much larger in Long et al. (2018) than in Clarke et al. (2018). This discrepancy is probably due to the limited spatial resolution of our observations compared to Clarke et al. (2018) (at the distance of CI Tau, 19 and 9 au, respectively) which is most important for the innermost ring, located at ~ 14 au. For consistency, in this paper we will always refer to the gap widths as measured by Long et al. (2018), keeping in mind that the width of the innermost gap in CI Tau might have been strongly overestimated.

The width of the two outer gaps in CI Tau corresponds to ~ 5 and 7 times the Hills radius of the planets used by Clarke et al. (2018) in their modelling. Thus, in the following, by averaging the results from hydrodynamical simulations of CI Tau and MWC 480, we will assume that the gap width Δ scales as

$$\Delta = 5.5 R_H. \quad (2)$$

We remind the reader that the relation above is related to the gap in the dust radial profile, which may be different than the gas gap (which we do not consider in this paper). The resulting planet masses calculated with equation (2) for the 15 gaps in our sample are reported in Table 1.

The stellar masses are reproduced from those adopted by Long et al. (in preparation), obtained from a combination of dynamical mass measurements, when available (Simon, Dutrey & Guilloteau 2000; Piétu, Dutrey & Guilloteau 2007; Guilloteau et al. 2014; Simon et al. 2017), and otherwise by comparing literature estimates of temperature and luminosity to a combination of the Baraffe et al. (2015) and nonmagnetic models of Feiden (2016), as applied by Pascucci et al. (2016). UZ Tau E is a spectroscopic binary (e.g. Prato et al. 2002) and therefore has a dynamical mass that is much higher than would be expected from its spectral type.

In the plots shown below we also include error bars on the inferred planet masses coming from the uncertainty in the proportionality factor, ranging from 4.5 to 7 (Rosotti et al. 2016), resulting in an uncertainty in the inferred planet mass of the order of a factor ~ 2 either side, which dominates over the uncertainty on the assumed stellar mass.

Table 1. Gap properties used in this study (from Long et al. 2018). The columns indicate, respectively: (1) star name; (2) gap width over gap location; (3) gap location with uncertainties from Long et al. (2018); (4) stellar mass; (5) total mm-flux at 1.3 mm of source; (6) total dust mass from mm-flux; and (7) inferred planet mass.

(1) Star name	(2) Δ/R	(3) R/au	(4) M_*/M_\odot	(5) F_ν/mJy	(6) $M_{\text{dust}}/M_{\text{Jup}}$	(7) M_p/M_{Jup}
RY Tau	0.129	43.41 ± 0.13	$2.04^{+0.3}_{-0.26}$	210.39	0.29	0.077
UZ Tau E	0.115	69.05 ± 0.2	$1.23^{+0.08}_{-0.08}$	129.52	0.19	0.023
DS Tau	0.724	32.93 ± 0.32	$0.83^{+0.02}_{-0.02}$	22.24	0.048	5.6
FT Tau	0.297	24.78 ± 0.19	$0.34^{+0.17}_{-0.09}$	89.77	0.12	0.15
MWC480	0.329	73.43 ± 0.16	$2.1^{+0.06}_{-0.06}$	267.76	0.59	1.3
DN Tau	0.083	49.29 ± 0.44	$0.87^{+0.17}_{-0.14}$	88.61	0.125	0.009
GO Tau	0.239	58.91 ± 0.66	$0.49^{+0.01}_{-0.01}$	54.76	0.097	0.057
GO Tau	0.258	86.99 ± 0.88	$0.49^{+0.01}_{-0.01}$	54.76	0.097	0.07
IQ Tau	0.171	41.15 ± 0.63	$0.74^{+0.01}_{-0.01}$	64.11	0.094	0.065
DL Tau	0.182	39.29 ± 0.32	$1.02^{+0.02}_{-0.02}$	170.72	0.37	0.11
DL Tau	0.166	66.95 ± 0.87	$1.02^{+0.02}_{-0.02}$	170.72	0.37	0.08
DL Tau	0.262	88.9 ± 1.11	$1.02^{+0.02}_{-0.02}$	170.72	0.37	0.33
CI Tau	0.987	13.92 ± 0.32	$0.91^{+0.02}_{-0.02}$	142.4	0.33	15.7
CI Tau	0.281	48.36 ± 0.41	$0.91^{+0.02}_{-0.02}$	142.4	0.33	0.36
CI Tau	0.284	118.99 ± 0.65	$0.91^{+0.02}_{-0.02}$	142.4	0.33	0.37

Note that the outcome of hydrodynamical simulations of gas and dust with embedded planets depends on several physical and numerical parameters, including assumptions on the dust–gas coupling, the detailed treatment of the gas thermodynamics (locally isothermal equations of state are often used), the use of two-dimensional or three-dimensional codes, etc. All such assumptions imply an uncertainty in the relation between planet mass and width of the dust gap induced by it, often difficult to quantify. In this paper, we have simply assumed it to be given (see above) by the deviation between the different determination made by different groups using different codes and specific set-ups, although we warn that some of these uncertainties might be systematic (for example, most codes make the same assumptions on the thermodynamics, which may tend to overestimate the gap width for a given planet mass), and thus shared between all of the various simulations.

3 RESULTS

Fig. 1 shows a comparison between masses and locations of currently known exo-planets (empty circles, data from www.exoplanet.net, as of the 2018 Oct 31) and those inferred from the gap extents in Long et al. (2018) (red points) using equation (2). Recently, the DSHARP ALMA Large Program data have been released, with an analysis of additional gaps in bright protostellar discs. Zhang et al. (2018) measured the width¹ of 19 gaps, from which we calculate the putative planet mass with the same procedure as we used for the Long et al. (2018) sample, with stellar and disc parameters taken from Zhang et al. (2018). The resulting planet masses are shown with green points in Fig. 1 and are listed in Table 2. Despite the differences in estimating the planet masses, they appear to be consistent with those quoted by Zhang et al. (2018).

¹Note that Zhang et al. (2018) define the gap width in a slightly different way than us, so that $\Delta_{\text{Zhang}}/R = (R_{\text{out}} - R_{\text{in}})/R_{\text{out}}$, where $R_{\text{out, in}}$ are the outer/inner radius of the gap, which makes their gap size of the order of two times the one obtained with our definition. When using their sample, we have corrected their data for this difference.

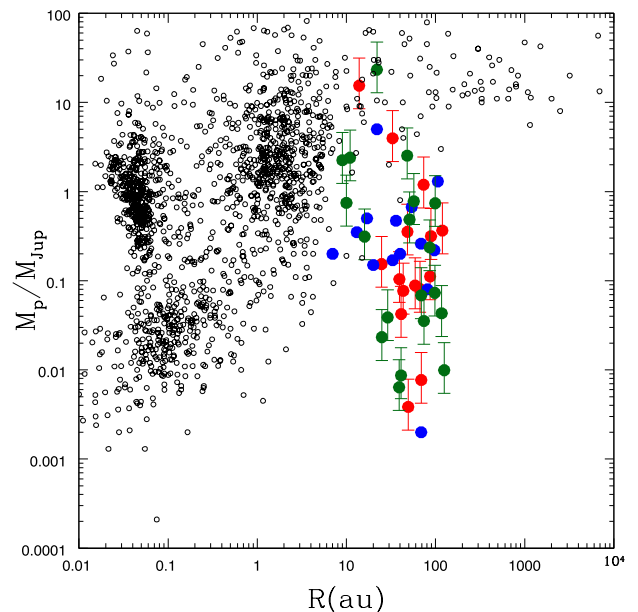


Figure 1. Plot of mass (y-axis) M_p versus separation from the central star R (x-axis) of the (empty circles) currently known exo-planets (retrieved from the exoplanet.org data base) compared to those obtained from the sample in Long et al. (2018) (red points) and Zhang et al. (2018) (green points) using equation (2), and those collected by Bae et al. (2018) (blue points). Error bars in the planet masses indicate the uncertainty in the proportionality factor between gap width and planet’s Hills radius, assumed to be in the range [4.5–7].

In addition, we also plot as blue circles the planet masses and locations inferred from other 14 ringed discs and disc hosting cavities (so-called transition discs), as collected by Bae, Pinilla & Birnstiel (2018) (see their Fig. 1). For the few cases (HD163296, Elias 24, and AS209) that are present both in the DSHARP and in the Bae et al. (2018) sample, we use the planet mass obtained from the measured gap width in DSHARP. We list the location and mass

Table 2. Planet masses for the gaps in the DSHARP survey (Zhang et al. 2018). The columns indicate, respectively: (1) star name; (2) gap width according to Zhang et al. (2018); (3) gap location; and (4) inferred planet mass.

(1) Star name	(2) Δ_{Zhang}/R	(3) R/au	(4) $M_{\text{p}}/M_{\text{Jup}}$
AS209	0.42	9	2.25
AS209	0.31	99	0.74
Elias 24	0.32	57	0.77
Elias 27	0.18	69	0.07
GW Lup	0.15	74	0.035
HD 142666	0.2	16	0.3
HD 143006	0.62	22	23
HD 143006	0.22	51	0.48
HD 163296	0.24	10	0.74
HD 163296	0.34	48	2.5
HD 163296	0.17	86	0.23
SR4	0.45	11	2.4
DoAr 25	0.15	98	0.07
DoAr 25	0.08	125	0.01
Elias 20	0.13	25	0.02
IM Lup	0.13	117	0.04
RU Lup	0.14	29	0.038
Sz 114	0.12	39	0.006
Sz 129	0.08	41	0.008

Table 3. Planet masses collected by Bae et al. (2018). The columns indicate, respectively: (1) star name; (2) gap location; and (3) inferred planet mass.

(1) Star name	(2) R/au	(3) $M_{\text{p}}/M_{\text{Jup}}$
HL Tau	13.1	0.35
HL Tau	33	0.17
HL Tau	68.6	0.26
TW Hya	20	0.15
TW Hya	81	0.08
HD 169142	54	0.67
HD 97048	106	1.3
Lk Ca 15	36	0.47
RXJ 1615	97	0.22
GY 91	7	0.2
GY 91	40	0.2
GY 91	69	0.002
V 4046	17	0.5
PDS 70	22	5

of the planets collected by Bae et al. (2018) in Table 3. In total, we thus have 48 planets inferred from the gaps in dusty discs, which is the largest gap sample analysed to date.

The inferred planet masses from our sample and the Zhang et al. (2018) sample are consistent with those of the Bae et al. (2018) sample, although we caution that the method used to derive them are significantly different: while the masses collected by Bae et al. (2018) are mostly inferred from hydrodynamical simulations, coupled with a dust evolution module, our estimates are based on a simpler approach. It is interesting to note, however, that the two approaches lead to compatible results.

The properties of the putative planets obtained with our method populate a region in the mass versus separation diagram that cannot be probed by the current exo-planet surveys. We note that the observations of planets at distances $\gtrsim 10$ au from the central star are biased towards large masses: at those separations planets can be detected mostly by direct imaging or by microlensing. Recent determinations of the occurrence rates of massive planets ($M >$

$2 M_{\text{Jup}}$) beyond 10–20 au are in the range of a few up to 5 per cent (Bowler & Nielsen 2018). More specifically, the 68 per cent confidence interval is estimated to be [1.6–5.1] per cent for 2–14 M_{Jup} planets between 8 and 400 au by Lannier et al. (2016), [4–10] per cent for 5–20 M_{Jup} planets between 10 and 1000 au by Meshkat et al. (2017) and [0.75–5.7] per cent for 0.5–75 M_{Jup} planets between 20 and 300 au by Vigan et al. (2017). Note, however, that such estimates suffer from very large uncertainties, depending on whether one uses a hot or a cold start model for the planet. For example, Stone et al. (2018), using a cold start model, put an upper limit to the occurrence rate of 7–10 M_{Jup} planets between 5 and 50 au as high as 90 per cent for FGK stars.

For the combined sample, including the Long et al. (2018), Zhang et al. (2018), and Bae et al. (2018) data the occurrence rate of such massive planets is $7/48 \sim 15$ per cent, which is slightly higher than the published rates. However, note that, apart from the Long et al. (2018) sample, the other gap detections all present strong biases to very luminous mm sources. Furthermore, it is important to note that these planets will naturally accrete mass and migrate to the inner disc during their evolution, and thus change their properties, see Section 3.1.

From the planet–disc interaction point of view, the minimum planet–star mass ratio able to carve a dust gap depends on the coupling between the gas and the dust, as measured by the Stokes number

$$\text{St} = \Omega t_{\text{stop}}, \quad (3)$$

where t_{stop} is the drag stopping time and Ω is the local Keplerian frequency (Weidenschilling 1977). In particular, for strongly coupled dust grains (with $\text{St} \ll 1$) the minimum dust gap opening planet mass is

$$\frac{M_{\text{min}}}{M_{\star}} = 0.3 \left(\frac{H}{R} \right)^3, \quad (4)$$

where H/R is the disc aspect ratio at the planet position, which depends on the disc temperature (Lambrechts, Johansen & Morbidelli 2014; Rosotti et al. 2016; Dipierro & Laibe 2017). If we consider a standard irradiated disc model (Chiang & Goldreich 1997; Dullemond, van Zadelhoff & Natta 2002; Armitage 2010), the disc aspect ratio is given by

$$\frac{H}{R} \approx 0.05 \left(\frac{R}{10 \text{ au}} \right)^{1/4}. \quad (5)$$

In practice, since we obtain the planet mass from the gap width by assuming that it scales with the planet Hill’s radius, the condition $M_{\text{p}} \gtrsim M_{\text{min}}$ implies (through equations 1–4) that

$$\frac{\Delta}{R} \gtrsim [2.1\text{--}3.2] \frac{H}{R} \quad (6)$$

for strongly coupled dust, where the brackets correspond to our chosen interval in the proportionality factor in equation (1) ($k = [4.5\text{--}7]$). For more loosely coupled dust grains ($\text{St} \gtrsim 1$), conversely, a dust gap can be opened relatively more easily because viscous and pressure forces are not effective in closing the gap. Combining equations (56) and (58) in Dipierro & Laibe (2017), we obtain in this case the requirement:

$$\frac{\Delta}{R} \gtrsim \text{St}^{-1/2} \frac{H}{R}. \quad (7)$$

Note that, for $\text{St} \leq 1$ the gap width cannot be smaller than the disc thickness H .

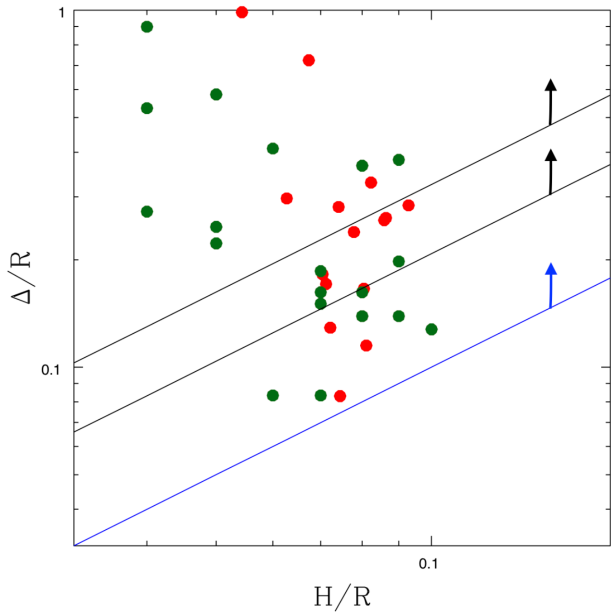


Figure 2. Measured gap widths versus disc aspect ratio (as estimated from equation 5) in the Long et al. (2018) (red points) and in the Zhang et al. (2018) (green points) samples. The two black lines indicate the range $[2.1\text{--}3.2]H/R$ above which the gap width is expected to lie if the dust is strongly coupled to the gas ($St \ll 1$). The blue line indicates the relation $\Delta = H$, that is the minimum gap width expected for dust with $St \sim 1$.

In Fig. 2, we plot the gap width Δ/R for the gaps in the two samples of Long et al. (2018) (red points) and Zhang et al. (2018) (green points) versus the disc aspect ratio at the gap location H/R , as computed from equation (5). The two black lines indicate the range $[2.1\text{--}3.2]H/R$ above which we should expect the gap width to lie, if the dust is strongly coupled to the gas. The blue line shows instead the simple relation $\Delta = H$, that is the minimum gap width expected for dust with $St \sim 1$. As we can see, most of our points are consistent with the dust being strongly coupled to the gas. In a few cases the gap width appears to be somewhat smaller, which may imply that in these systems the dust is less coupled and it is thus easier to open up a dust gap.

Next, we check for possible correlations between the derived planet mass and the disc dust mass, as measured from the mm flux, assuming optically thin emission, a dust temperature of $T_{\text{dust}} = 20$ K and a dust opacity² $\kappa = 2.3 (\nu/230 \text{ GHz})^{0.4} \text{ cm}^2 \text{ g}^{-1}$. This is plotted in Fig. 3, which shows the mass of the putative planets versus the total dust mass in the disc (Long et al. 2018). Apart from the two most massive planets (corresponding to the inner ring of CI Tau and to DS Tau), the rest of our small sample appears to follow a tentative trend. The solid line in Fig. 3 shows the best linear regression of the data (excluding the two outliers) in the form $M_p \propto M_{\text{dust}}^{1.33}$. Note that, of course, this plot relates the planet mass to the *current* dust mass in the disc, which does not necessarily represent a proxy for the disc mass *at the time of planet formation* (Nixon, King & Pringle 2018). Moreover, inferring the value of the dust mass from continuum observations of protoplanetary discs is still under debate, mostly due to uncertainty in dust opacity and optical depth

²Although note that the dust opacity values are very uncertain, as it depends on the local size distribution and composition of dust grains, that is controlled by grain growth and radial drift.

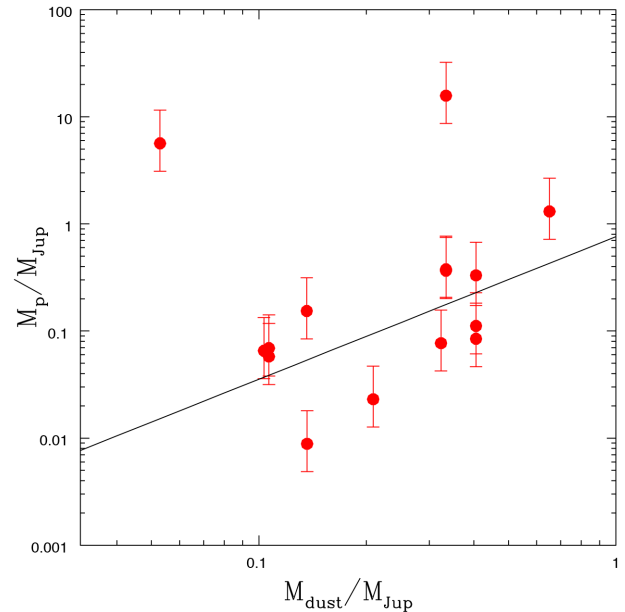


Figure 3. Mass of the planets M_p (y-axis) versus total dust mass in the disc (x-axis) for the putative planets in Long et al. (2018). The solid line indicates the linear regression of the form $M_p \propto M_{\text{dust}}^{1.33}$.

(Bergin & Williams 2018). Indeed, Manara, Morbidelli & Guillot (2018), using photometric data, have recently shown that the disc dust masses measured from mm fluxes may be in general lower than the mass of exo-planets (but see Mulders, Pascucci & Apai 2015 and Pascucci et al. 2016 for a different opinion, based on Kepler planet mass estimates), as also confirmed by spatially resolved studies (Tazzari et al. 2017), who find dust surface density profiles below the Minimum Mass Solar Nebula in their Lupus disc sample. This can be explained with either a rapid formation of planetary cores (Najita & Kenyon 2014), or a replenishment of the disc from the environment, or a sizable fraction of circumstellar dust being captured in larger dust agglomerations such as boulders, planetesimals, etc. Especially for the two most massive inferred planets in our sample, it is possible that most of the primordial disc mass might have already ended up in planets that thus might appear to live in less massive discs than the correlation would suggest.

In a sample of transition discs, Pinilla et al. (2018) did not find any correlation between mm-flux and cavity size. Note that although also in transition discs the cavity is sometimes interpreted as the effect of the presence of a planet, here we are not concerned with discs with cavities, but only in gaps.

Finally, in Fig. 4 we show the location of the gaps in our sample versus the stellar masses. No clear trend can be recognized here, indicating that, in the planet interpretation, the planet formation region does not appear to depend strongly on the stellar mass.

3.1 The fate of planets

Due to interactions between planets and the surrounding disc material, the properties of the putative planets inferred in gapped-like discs around young stellar objects are expected to evolve with time. As a result, the planets would generally migrate and accrete mass from the surrounding disc.

In order to predict if the planets will survive to their migration and to compare their final properties with those of currently known exo-planets, we compute the variation of the separation and mass

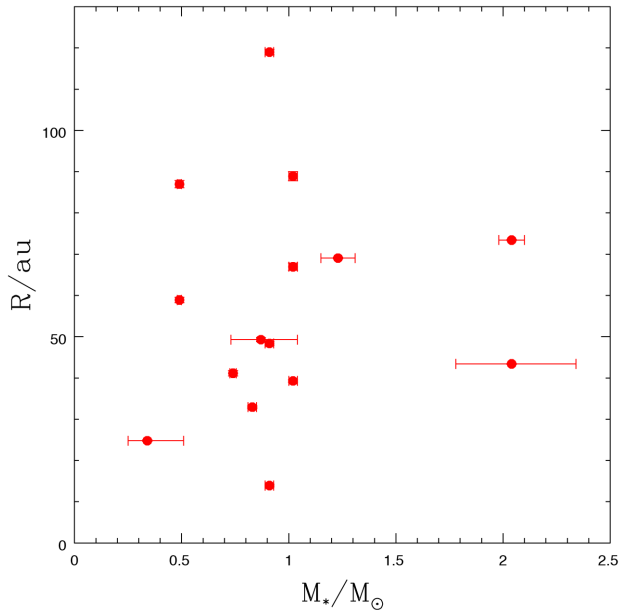


Figure 4. Scatter plot showing the gap location R (y-axis) versus the central star mass M_* (x-axis) for the putative planets in Long et al. (2018).

of the planets under consideration using prescribed migration and accretion laws, assuming that the disc properties are fixed in time. We assume that the planets migrate according to type I or type II migration regime (e.g. see Papaloizou & Terquem 2006), depending on their ability to carve a deep gap in the local gas density structure (as opposed to the dust gaps that we know have been opened in all of our putative planets). Starting from the initial properties of the planets (see Tables 1–3), we assume that the gap-opening mass $M_{p, \text{gap}}$ in the gas disc is given by the Crida, Morbidelli & Masset (2006) criterion, corresponding to a drop of the local gas surface density to a factor ~ 10 per cent of the unperturbed value, i.e.

$$\frac{3}{4} \frac{H}{R_H} + \frac{50 \alpha M_*}{M_{p, \text{gap}}} \left(\frac{H}{R} \right)^2 = 1, \quad (8)$$

where α indicates the Shakura–Sunyaev turbulence parameter (Shakura & Sunyaev 1973), assumed to be equal to 0.005 (Flaherty et al. 2017). The value of the aspect ratio at the planet position is obtained from equation (5). We adopt a simplistic bimodal model for planetary migration by assuming that planets with mass smaller (larger) than $M_{p, \text{gap}}$ migrate according to type I (II) regime.

The planet orbital evolution and accretion history are then computed following the method of Dipierro et al. (2018) (see their section 4.4 for details). In particular, we assume that low-mass planets (i.e. $M_p < M_{p, \text{gap}}$) initially undergo a rapid growth and migration phase (corresponding to the Type I regime, when the planet is still embedded in the disc), rapidly reaching a mass and radius given by equations (20)–(22) in Dipierro et al. (2018). Then, we let the planets migrate without growing in mass on the slower viscous time-scale of the disc:

$$t_{\text{migr, II}} = \frac{2}{3} \left(\frac{1}{\alpha \Omega} \right) \left(\frac{H}{R} \right)^{-2}. \quad (9)$$

Those planets in our sample with an initially high mass (i.e. $M_p > M_{p, \text{gap}}$) simply migrate towards the central star according to the type II regime. If the planet mass is much larger than the local disc mass, Type II migration is expected to be further slowed down by a factor $B = M_p / 4\pi \Sigma R^2$, where Σ is the total (gas + dust) disc surface

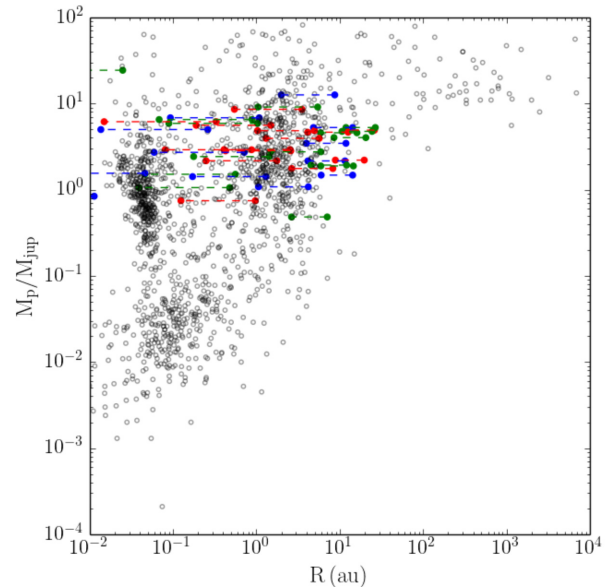


Figure 5. Same as Fig. 1 but where the points indicate the expected final mass and location of the putative planets inferred in Long et al. (2018) (red), Zhang et al. (2018) (green), and Bae et al. (2018) (blue) after 3 and 5 Myr of planet evolution. The dashed lines indicate the range of planet locations after a total time in the range [3,5] Myr. Planetary accretion and migration lead to a redistribution of planet properties that mostly populates the branch of cold Jupiters.

density (Ivanov, Papaloizou & Polnarev 1999). However, given that the dust masses for our sample (see Table 1) are generally of the order of the estimated planet mass, and assuming a gas-to-dust ratio of 100, we find that none of our planets is massive enough to be in this modified Type II migration regime.

Fig. 5 shows the final properties (separation from the central star and mass) of the planets in our sample. The dashed lines indicate the range of planet locations after a total time in the range [3,5] Myr (taken to be an estimate of the gas disc lifetime, including a possible spread in ages and evolutionary time), compared to those inferred from the currently known exo-planets. Initially, around half of the planets in our sample have a mass below the one given by the gas gap-opening criterion and therefore accrete mass and migrate in type I regime. We find that these migrating and accreting planets will reach the gap opening mass (equation 8) and transit into the slow type II migration regime well before being lost into the central star (and thus save themselves from rapid migration), consistently with recent findings of Crida & Bitsch (2017) and Johansen, Ida & Brasser (2018). More massive planets (i.e. $M_p > M_{p, \text{gap}}$) simply slowly migrate towards the central star according to the type II regime. After planetary migration and accretion, ~ 20 per cent of the planets are lost into the star (we assume that a planet is lost into the star if its separation is smaller than 0.01 au). Moreover, nearly all of the planets in our sample reach a mass above Jupiter.

Our evolutionary model is very simplified and approximated: we have kept the disc properties fixed during the evolution, we have simply assumed a uniform lifetime for all the discs (neglecting also a possible range in ages in our sample) and we have neglected possible modifications to the migration laws (e.g. Ivanov et al. 1999; Dürmann & Kley 2015). However, it is interesting to note that the final distribution of the planets is consistent with the known properties of the exo-planet population, especially those placed in the branch of cold Jupiters.

Since the planetary growth and migration are closely linked to the disc evolution, a proper investigation should take into account the underlying evolution of the dynamical and thermal structure of the gas and dust content in protoplanetary discs, along with the possible presence of mechanisms acting to slow-down (or even reverse) the inward planet migration such as photoevaporation (Matsuyama, Johnstone & Murray 2003; Alexander & Pascucci 2012), migration in a multiple planet system (Martin et al. 2007), disc migration feedback (Fung & Lee 2018), sublimation lines, shadowed regions and heat transition barriers (e.g. Bitsch et al. 2015; Baillié, Charnoz & Pantin 2016; Johansen et al. 2018; Ndugu, Bitsch & Jurua 2018), and even further migration occurring by planet–planet interaction after the disc is dispersed.

4 CONCLUSIONS

In this paper, we have analysed the sample of rings and gaps observed to date in protoplanetary discs to infer the properties of the population of planets that might have been able to carve the observed gaps. Our analysis includes the recent detections of gaps in discs in the Taurus star-forming region by Long et al. (2018), along with the recent observations in the DSHARP ALMA Large Program analysed by Zhang et al. (2018) and the additional sample of gaps collected by Bae et al. (2018). For those discs where a proper hydrodynamical modelling was not carried out to infer the planet properties, we estimate the putative planet masses assuming that the gap width is proportional to the planet Hill’s radius. We then describe some possible correlations of the putative planet properties with the other system parameters.

The most important conclusion of our work is that there appears to be no discrepancy between the possibility that embedded planets are responsible for carving gaps in discs around young stars and the lack of detections at similar locations by dedicated planet searches. First, we find that the locations and masses of the planets around these young stars occupy a distinct region in the planet mass versus semimajor axis plane that is presently not probed by planet detection campaigns (around both young, T Tauri stars and older, main-sequence stars). The high frequency of gaps observed in planet forming discs has sometimes been interpreted as evidence against a planet induced model for gap formation, based on the fact that planet detection campaigns do not observe massive planets at tens of au very frequently. Our analysis, however, shows that if the planets remain at the lower end of the masses required to create gaps then they would be, as yet, undetectable by campaigns searching at these distances.

The number of gaps in the sample of Long et al. (2018) (which is the least biased sample of gaps in discs available so far) is 15 out of 32 targets. Taking into account the fraction of disc hosting stars in Taurus, which is 0.75 (Luhman et al. 2010), this leads to an occurrence rate of gaps around young stars of 35 per cent. Fernandes et al. (2019) have compared favourably this number with their estimate of the number of giant planets (with masses in the $[0.1\text{--}20] M_{\text{Jup}}$ range and semimajor axis in the $[0.1\text{--}100]$ au range), which is 26.6 per cent. A similar occurrence rate from RV surveys has also been published by Cumming et al. (2008), who estimate a value of 17–20 per cent for giant planets (above Saturn mass) within 20 au. However, one must remember that the occurrence rates of giant planets from RV surveys or direct imaging should not be directly compared with the occurrence rates of gaps, because planets migrate and accrete mass during the disc evolution.

Motivated by this, we further explore the final properties of the planets in our sample by using a simple prescription of planetary

migration and accretion (Dipierro et al. 2018). After 3–5 Myr of planetary evolution, we find that the final properties of the planets approach the branch of cold Jupiters in the current observed distribution of exoplanets. Thus, planetary migration and accretion provide a second explanation for the lack of detected planets at large distances around older, main-sequence stars.

After planetary migration and accretion, ~ 20 per cent of the planets are lost into the star. However, for the subsample including only Long et al. (2018) discs, only one planet is lost and the final number of surviving planets is 14, most of them having masses above Jupiter. In total, thus, the occurrence rate of Jupiter mass planets in our model is 33 per cent. As mentioned above, Fernandes et al. (2019) estimate a value of 26.6 per cent for the occurrence rate of giants (with masses above $0.1 M_{\text{Jup}}$), but this number is reduced to only 6 per cent for Jupiter mass planets, according to Fernandes et al. (2019). This interesting fact can be explained in several different ways. First, we note that our estimates are certainly affected with low-number statistic uncertainties, and future, unbiased larger surveys should improve in this respect. Secondly, it is worth noting that planet detection campaigns concentrate on Solar type stars, while this is not the case for the disc surveys, which include a wider range of stellar types. Thirdly, our planetary accretion model probably overestimates the amount of accreted mass. Indeed, we assume an isothermal equation of state to compute the accretion rate (Dipierro et al. 2018), which is the maximum accretion rate allowed (Ayliffe & Bate 2009; Szulágyi 2015; Szulágyi et al. 2016; Lambrechts & Lega 2017). Certainly, this kind of comparison can put interesting constraints on accretion and migration models.

Estimating the presence of a planet based on the gap it carves in the protoplanetary disc naturally has a bias in that very low mass planets do not induce gaps. Such a bias can be quantified using known relationships between the minimum gap opening planet mass (and thus the minimum expected gap width) and the disc aspect ratio. Our results show that the measured gap widths are generally larger than a few times the disc thickness H , which is consistent with predictions for planet gap opening for a dust population strongly coupled to the gas. In a few cases, the gap width is comparable to H , which might imply that the dust–gas coupling in these systems is lower. However, these gaps are still consistent with $St \gtrsim 1$ for the mm-sized grains, as required for them to remain at their current location and not undergo rapid inward drift. In no cases do we find gap widths smaller than H , which strongly supports our hypothesis that the observed gaps are opened by planets.

Despite uncertainties coming from the small size of our sample (and by the presence of a couple of outliers), we suggest that there could be a correlation between planet mass and disc mass, as inferred from the disc mm flux, supporting the notion that more massive discs tend to produce more massive planets. However, note that a similar correlation between mm flux and cavity size was not found for the larger cavities (as opposed to the gaps discussed here) around transition discs, analysed by Pinilla et al. (2018). No correlation is instead found between the location of the gaps and the stellar mass, possibly indicating that the planet formation region does not appear to depend strongly on stellar mass, although again note that this might be affected by the relatively small sample size.

Upcoming surveys of discs will certainly add more data points to our currently small sample and further refine or reject our findings. Importantly, theoretical models have developed to the point of making a priori predictions for exo-planet demographics. In general, analyses such as ours, once the samples are more complete, will be needed to relate the properties of newborn planets with the ‘adult’

planet population coming from planet detection campaigns around main-sequence stars, thus posing important constraints on the early evolution of planets in their discs.

ACKNOWLEDGEMENTS

We thank an anonymous referee for their insightful comments. We thank Jaehan Bae for providing us with masses and separations from the central star collected in Bae et al. (2018). GL, ERa, BN, and ERi acknowledge support by the project PRIN-INAF 2016 The Cradle of Life - GENESIS-SKA (General Conditions in Early Planetary Systems for the rise of life with SKA). This project has received funding from the European Union's Horizon 2020 research and innovation programme under the Marie Skłodowska-Curie grant agreement No 823823 (Dustbusters RISE project). GD and ERa acknowledge financial support from the European Research Council (ERC) under the European Union's Horizon 2020 research and innovation programme (grant agreement No 681601). MT has been supported by the DISCSIM project, grant agreement 341137 funded by the European Research Council under ERC-2013-ADG and by the UK Science and Technology research Council (STFC). DJ is supported by the National Research Council of Canada and by an NSERC Discovery Grant. FME, GvdP, YB acknowledge funding from ANR of France (contract ANR-16-CE31-0013, Planet-Forming-Discs). FL and GJH are supported by general grants 11773002 and 11473005 awarded by the National Science Foundation of China. CFM acknowledges an ESO Fellowship and was partly supported by the Deutsche Forschungs-Gemeinschaft (DFG, German Research Foundation) - Ref no. FOR 2634/1 TE 1024/1-1, by the DFG cluster of excellence Origin and Structure of the Universe (www.universe-cluster.de).

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¹*Dipartimento di Fisica, Università degli Studi di Milano, Via Celoria 16, I-20133 Milano, Italy*

²*Department of Physics and Astronomy, University of Leicester, Leicester LE1 7RH, UK*

³*Kavli Institute for Astronomy and Astrophysics, Peking University, Yiheyuan 5, Haidian Qu, 100871 Beijing, China*

⁴*Lunar and Planetary Laboratory, University of Arizona, Tucson, AZ 85721, USA*

⁵*Earths in Other Solar Systems Team, NASA Nexus for Exoplanet System Science, USA*

⁶*Department of Astronomy/Steward Observatory, The University of Arizona, 933 North Cherry Avenue, Tucson, AZ 85721, USA*

⁷*European Southern Observatory, Karl-Schwarzschild-Str. 2, D-85748 Garching bei München, Germany*

⁸*Institute of Astronomy, University of Cambridge, Madingley Road, Cambridge CB3 0HA, UK*

⁹*Max Planck Institute for Astronomy, Königstuhl 17, D-69117 Heidelberg, Germany*

¹⁰*Purple Mountain Observatory & Key Laboratory for Radio Astronomy, Chinese Academy of Sciences, 2 West Beijing Road, Nanjing 210008, China*

¹¹*Department of the Geophysical Sciences, The University of Chicago, Chicago, IL 60637, USA*

¹²*Leiden Observatory, Leiden University, P.O. box 9513, NL-2300 RA Leiden, The Netherlands*

¹³*Univ. Grenoble Alpes, CNRS, IPAG, F-38000 Grenoble, France*

¹⁴*NRC Herzberg Astronomy and Astrophysics, 5071 West Saanich Road, Victoria, BC V9E 2E7, Canada*

¹⁵*Department of Physics and Astronomy, University of Victoria, Victoria, BC, V8P 5C2, Canada*

¹⁶*Vassar College Physics and Astronomy Department, 124 Raymond Avenue, Poughkeepsie, NY 12604, USA*

¹⁷*Sorbonne Université, Observatoire de Paris, Université PSL, CNRS, LERMA, F-75014 Paris, France*

¹⁸*Five College Astronomy Department, Smith College, Northampton, MA 01063, USA*

¹⁹*Space Telescope Science Institute Baltimore, MD 21218, USA*

²⁰*INAF-Osservatorio Astronomico di Roma, via di Frascati 33, I-00040 Monte Porzio Catone, Italy*

²¹*INAF-Osservatorio Astronomico di Padova, Vicolo dell'Osservatorio 5, I-35122 Padova, Italy*

²²*NASA Ames Research Center and Bay Area Environmental Research Institute, Moffett Field, CA 94035, USA*

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